

Exhibit No. 2

Reradiation Analysis

Approach

The approach taken for this analysis is to meet the NTIA requirements is as follows:

1. Determine the power density required to generate -140 dBm at a GPS input terminal (maximum power allowable) when connected to an isotropic antenna.
2. Determine the power density at 100 ft (~30 m) from our reradiating antenna systems. As each of the antennas will be located near the building wall, this calculation will meet the NTIA requirement showing compliance with the -140 dBm limit 100 feet from the building.
3. Determine the safety margin at 100 ft (~30m) referencing the -140 dBm requirement.

Maximum Power Allowable

The maximum allowable power at a GPS receiver is -140 dBm when connected to an isotropic antenna.

$$-140 \text{ dBm} = 1 \times 10^{-17} \text{ W}$$

To determine the maximum allowable power density (P_d) at an antenna, it is known that:

$$P_d \times (\text{Effective Area}) = \text{Receiver Power}$$

Therefore,

$$\text{Maximum } P_d = \text{Max Allowable Receiver Power} / (\text{Antenna Effective Area})$$

Given that the Antenna Effective Area of an isotropic antenna is $\lambda^2/4\pi$,

Then for **1574.42 MHz (L1):**

$$\text{Effective Area} = (0.191\text{m})^2/4\pi = 2.90 \times 10^{-3} \text{ m}^2$$

And for **1277.60 MHz (L2):**

$$\text{Effective Area} = (0.244\text{m})^2/4\pi = 4.74 \times 10^{-3} \text{ m}^2$$

Therefore, the maximum allowable power density for -140 dBm at a GPS receiver is:

At **1574.42 MHz (L1):**

$$(P_d)_{\text{max}} = 1 \times 10^{-17} \text{ W} / 2.9 \times 10^{-3} \text{ m}^2 = 3.45 \times 10^{-15} \text{ W/m}^2$$

At **1277.60 MHz (L2):**

$$(P_d)_{\text{max}} = 1 \times 10^{-17} \text{ W} / 4.74 \times 10^{-3} \text{ m}^2 = 2.11 \times 10^{-15} \text{ W/m}^2$$

AGS LRLAP Lab (Bldg NA) Transmit Power Calculations

The calculations apply to all antenna operating in building NA.

The maximum transmit antenna Gain (G) within 30° of horizontal is:

$$G = +0.9 \text{ dBic} = 1.23 \text{ (numeric)}$$

The Measured Power (T_x) over 25 MHz at the antenna input is:

$$\text{For } \mathbf{1574.42 \text{ MHz (L1):}} \quad T_{L1} = -99.5 \text{ dBm} = -129.5 \text{ dBw} = 1.122 \times 10^{-13} \text{ W}$$

$$\text{And for } \mathbf{1277.60 \text{ MHz (L2):}} \quad T_{L2} = -103.5 \text{ dBm} = -133.5 \text{ dBw} = 4.47 \times 10^{-14} \text{ W}$$

The Power Density (P_d) is:

$$P_d = T_x G / 4\pi r^2$$

Therefore, the Power Density at 100 ft (~30 m) and within 30° of horizontal is:

At **1574.42 MHz (L1):**

$$P_d = (1.122 \times 10^{-13} \text{ W})(1.23) / 4\pi(30)^2 = 1.22 \times 10^{-17} \text{ W/m}^2$$

At **1277.60 MHz (L2):**

$$P_d = (4.47 \times 10^{-14} \text{ W})(1.23) / 4\pi(30)^2 = 4.86 \times 10^{-18} \text{ W/m}^2$$

The **worst case** maximum transmit antenna Gain (G) at 90° of horizontal is:

$$G = +5.0 \text{ dBic} = 3.16 \text{ (numeric)}$$

Therefore, the **worst case** Power Density at 100 ft (~30 m) and at 90° of horizontal is:

At **1574.42 MHz (L1):**

$$P_d = (1.122 \times 10^{-13} \text{ W})(3.16) = 3.14 \times 10^{-17} \text{ W/m}^2$$

At **1277.60 MHz (L2):**

$$P_d = (4.47 \times 10^{-14} \text{ W})(3.16) = 1.25 \times 10^{-17} \text{ W/m}^2$$

Nominal Power Density

Worst Case Power Density

Note 1: Power measurements were taken with a spectrum analyzer using a low noise pre-amplifier and are the maximum power across the 25 MHz Bandwidth. These measurements were taken at the coax terminal that connects to the transmit (or reradiating) antenna.

AGS LRLAP Portable (Dynamics Lab) Transmit Power Calculations

The maximum transmit antenna Gain (G) within 30° of horizontal is:

$$G = +0.9 \text{ dBic} = 1.23 \text{ (numeric)}$$

The Measured Power (T_x) over 25 MHz at the antenna input is:

$$\text{For } \mathbf{1574.42 \text{ MHz (L1):}} \quad T_{L1} = -99.5 \text{ dBm} = -129.5 \text{ dBw} = 1.122 \times 10^{-13} \text{ W}$$

$$\text{And for } \mathbf{1277.60 \text{ MHz (L2):}} \quad T_{L2} = -101.5 \text{ dBm} = -131.5 \text{ dBw} = 7.08 \times 10^{-14} \text{ W}$$

The Power Density (P_d) is:

$$P_d = T_x G / 4\pi r^2$$

Therefore, the Power Density at 100 ft (~30 m) and within 30° of horizontal is:

At **1574.42 MHz (L1):**

$$P_d = (1.122 \times 10^{-13} \text{ W})(1.23) = 1.22 \times 10^{-17} \text{ W/m}^2$$

At **1277.60 MHz (L2):**

$$P_d = (7.08 \times 10^{-14} \text{ W})(1.23) = 7.70 \times 10^{-18} \text{ W/m}^2$$

The **worst case** maximum transmit antenna Gain (G) at 90° of horizontal is:

$$G = +5.0 \text{ dBic} = 3.16 \text{ (numeric)}$$

Therefore, the **worst case** Power Density at 100 ft (~30 m) and at 90° of horizontal is:

At **1574.42 MHz (L1):**

$$P_d = (1.122 \times 10^{-13} \text{ W})(3.16) = 3.14 \times 10^{-17} \text{ W/m}^2$$

At **1277.60 MHz (L2):**

$$P_d = (7.08 \times 10^{-14} \text{ W})(3.16) = 1.98 \times 10^{-17} \text{ W/m}^2$$

Nominal Power Density

Worst Case Power Density

Transmit Power Calculation Summary

From Page 1 of this exhibit, we identified that the Antenna Effective Area of an isotropic antenna is $\lambda^2/4\pi$,

Then for **1574.42 MHz (L1):**

$$\text{Effective Area} = (0.191 \text{ m})^2 / 4\pi = 2.90 \times 10^{-3} \text{ m}^2$$

And for **1277.60 MHz (L2):**

$$\text{Effective Area} = (0.244 \text{ m})^2 / 4\pi = 4.74 \times 10^{-3} \text{ m}^2$$

Therefore, the **worst case** maximum equivalent isotropically radiated power at a distance of 100 feet (30 meters) from the building where the test is being conducted is as follows:

At 1574.42 MHz (L1):

$$(3.14 \times 10^{-17} \text{ W/m}^2)(2.90 \times 10^{-3} \text{ m}^2) = 9.11 \times 10^{-20} \text{ W or } -190 \text{ dB}_w \Rightarrow -160 \text{ dB}_m$$

At 1277.60 MHz (L2):

$$(1.98 \times 10^{-17} \text{ W/m}^2)(4.74 \times 10^{-3} \text{ m}^2) = 9.39 \times 10^{-20} \text{ W or } -190 \text{ dB}_w \Rightarrow -160 \text{ dB}_m$$

Both of which are no greater than the requirement of -140 dBm/24 MHz at a distance of 100 feet (30 meters) from the building where the test is being conducted.